

De Broglie hypothesized that the linear momentum and wavelength of a free massive particle are related by which of the following constants?

- (A) Planck's constant
- (B) Boltzmann's constant
- (C) The Rydberg constant
- (D) The speed of light
- (E) Avogadro's number

An atom has filled $n = 1$ and $n = 2$ levels. How many electrons does the atom have?

- (A) 2
- (B) 4
- (C) 6
- (D) 8
- (E) 10

In the Bohr model of the hydrogen atom, the linear momentum of the electron at radius r_n is given by which of the following? (n is the principal quantum number.)

- (A) $n\hbar$
- (B) $nr_n\hbar$
- (C) $\frac{n\hbar}{r_n}$
- (D) $n^2r_n\hbar$
- (E) $\frac{n^2\hbar}{r_n}$

A quantum mechanical harmonic oscillator has an angular frequency ω . The Schrödinger equation predicts that the ground state energy of the oscillator will be

- (A) $-\frac{1}{2}\hbar\omega$
- (B) 0
- (C) $\frac{1}{2}\hbar\omega$
- (D) $\hbar\omega$
- (E) $\frac{3}{2}\hbar\omega$

Consider a set of wave functions $\psi_i(x)$. Which of the following conditions guarantees that the functions are normalized and mutually orthogonal? (The indices i and j take on the values in the set $\{1, 2, \dots, n\}$.)

- (A) $\psi_i^*(x)\psi_j(x) = 0$
- (B) $\psi_i^*(x)\psi_j(x) = 1$
- (C) $\int_{-\infty}^{\infty} \psi_i^*(x)\psi_j(x)dx = 0$
- (D) $\int_{-\infty}^{\infty} \psi_i^*(x)\psi_j(x)dx = 1$
- (E) $\int_{-\infty}^{\infty} \psi_i^*(x)\psi_j(x)dx = \delta_{ij}$

The lifetime for the $2p \rightarrow 1s$ transition in hydrogen is 1.6×10^{-9} s. The natural line width for the radiation emitted during the transition is approximately

- (A) 100 Hz
- (B) 100 kHz
- (C) 100 MHz
- (D) 100 GHz
- (E) 100 THz

Consider a single electron atom with orbital angular momentum $L = \sqrt{2}\hbar$. Which of the following gives the possible values of a measurement of L_z , the z -component of L ?

- (A) 0
- (B) $0, \hbar$
- (C) $0, \hbar, 2\hbar$
- (D) $-\hbar, 0, \hbar$
- (E) $-2\hbar, -\hbar, 0, \hbar, 2\hbar$

Characteristics of the quantum harmonic oscillator include which of the following?

- I. A spectrum of evenly spaced energy states
 - II. A potential energy function that is linear in the position coordinate
 - III. A ground state that is characterized by zero kinetic energy
 - IV. A nonzero probability of finding the oscillator outside the classical turning points
- (A) I only
 - (B) IV only
 - (C) I and IV only
 - (D) II and III only
 - (E) I, II, III, and IV

Which of the following expressions is proportional to the total energy for the levels of a one-electron Bohr atom? (m is the reduced mass, Z is the number of protons in the nucleus, $-e$ is the charge on the electron, and n is the principal quantum number.)

- (A) $\frac{mZe^2}{n}$
- (B) $\frac{mZe^2}{n^2}$
- (C) $\frac{mZ^2e^4}{n^2}$
- (D) $\frac{m^2Z^2e^2}{n^2}$
- (E) $\frac{m^2Z^2e^4}{n^2}$

Which of the following statements about bosons and/or fermions is true?

- (A) Bosons have symmetric wave functions and obey the Pauli exclusion principle.
- (B) Bosons have antisymmetric wave functions and do not obey the Pauli exclusion principle.
- (C) Fermions have symmetric wave functions and obey the Pauli exclusion principle.
- (D) Fermions have antisymmetric wave functions and obey the Pauli exclusion principle.
- (E) Bosons and fermions obey the Pauli exclusion principle.

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D